BBN with light dark matter

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Abstract. Effects of light millicharged dark matter particles on primordial nucleosynthesis are considered. It is shown that if the mass of such particles is much smaller than the electron mass, they lead to strong overproduction of Helium-4. An agreement with observations can be achieved by non-vanishing lepton asymmetry. Baryon-to-photon ratio at BBN and neutrino-to-photon ratio both at BBN and at recombination are noticeably different as compared to the standard cosmological model. The latter ratio and possible lepton asymmetry could be checked by Planck. For higher mass of new particles the effect is much less pronounced and may even have opposite sign.

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1 Introduction

During the last year there arose renewed interest to the impact of possible light dark matter particles on Big Bang Nucleosynthesis (BBN) and Cosmic Microwave Background radiation (CMB) [1–3]. The interest was stimulated by an observation that the number of the effective neutrino species at BBN is possibly larger than that predicted by the standard model, $N_{eff} = 3.046$ (see e.g. Ref. [4]). Indeed, according to the analysis of the Helium-4 abundance $N_{eff} = 3.7^{+0.8}_{-0.7}$ [5]. This unknown relativistic form of matter got the name dark radiation.

The effect of additional particles on light element abundances is model dependent and may lead both to a rise and to a decrease of N_{eff} . This has been already found in earlier works with MeV dark matter particles [6, 7]. It was argued [7] that if the new particles, X, are in thermal equilibrium with neutrinos they would lead to an increase of the Helium-4 fraction for $m_X \leq 10$ MeV, while if they are in equilibrium with electrons, positrons and photons their effect is opposite. In the first case they correspond to an increase of N_{eff} and in the second case N_{eff} becomes lower.

In this paper we also consider an impact of new light particles on BBN. It is assumed that X-particles have a small electric charge, much smaller than the charge of electron, $e' \ll e$. We consider both cases of $m_X < m_e$ and $m_X > m_e$. The model with $m_X > m_e$ has been considered in detail previously [7]. In this paper we concentrate on the case $m_X < m_e$. As we shall see in what follows, during the BBN epoch these dark matter particles were in thermal equilibrium with e^+ , e^- , and photons and decoupled from neutrinos. Annihilation of e^+e^- pairs proceeds both into photons and into dark matter pairs, $X\bar{X}$. Later on the bulk of dark matter particles annihilates into photons. Here we consider the model where this happens after BBN, but of course this should occur long before hydrogen recombination to avoid strong constraints on CMBR spectrum distortions. Light elements abundances in this model are altered because of:

i) Increased Universe expansion rate during BBN;

- ii) Increased neutrino temperature with respect to the photon temperature because the entropy released in e^+e^- -annihilation is now distributed between photons and X-particles;
- iii) Increased baryon-to-photon ratio during BBN.

We will treat the influence of these factors on BBN analytically, and then calculate numerically in Sec. 3. But first let us define the presently allowed range of parameters of the model.

2 Existing constraints on milli-charged particles

We start with the review of existing bounds on the mass and electromagnetic coupling, α' , of milli-charged particles, in the range were they can be a (part of) dark matter.

2.1 Laboratory bounds

For $m_X < m_e$ the best particle physics bound on α' follows from the data on positronium decay to three photons [9], according to which $e' < 3.4 \cdot 10^{-5} \, e$, that is $\alpha_{11} \equiv 10^{11} (e')^2 / 4\pi < 1$, see also ref. [10], where the similar limit was obtained. For very light particles, $m_X < 1$ keV, the best experimental limit $e' < 10^{-5} \, e$ comes from the reactor experiments, [11]. Heavier X-particles, $m_X > m_e$, are less restricted, e.g. for $m_X = 100$ MeV the bound is $\alpha' < 3 \cdot 10^{-9}$ [10]. Stringent constraints on a MeV scale dark matter are provided by the fixed target experiments, in particular by the LSND [12], see Ref. [13] for a detailed discussion. Corresponding bounds may not be applicable to our model because extra light vector boson is not necessarily present and we do not aim to explain 0.511 keV annihilation line. For the milli-charged scalar particles the main reaction to consider is $\pi^0 \to \gamma + X\bar{X}$. Branching of this process will be of order α' , i.e. the number of produced X particles will be α' times the number of produced neutrino. X particles scatter in the detector with the cross-section $\alpha' = \alpha' / E^2$. It will be comparable to the weak cross-section at $(E/\text{GeV})^4 \sim 10^{10} \alpha (\alpha')^2 \sim 10^{-14} \alpha_{11}^2$, i.e. at $E < \text{MeV} \sqrt{\alpha_{11}}/3$, which looks safe.

2.2 Constraints from stellar evolution

The consideration of stellar cooling also allows to restrict the interaction strength of light X-particles [14]. These particles could be abundantly produced in stellar cores and if their mean free path is shorter than the stellar radius, they would efficiently carry out stellar energy, strongly amplify the stellar luminosity, and diminish the star age. Inside the Sun they could be created in the process $ee \to eeX\bar{X}$. The cross-section of this reaction can be roughly estimated as $\sigma(ee \to eeX\bar{X}) \sim \alpha^3 \alpha'/m_2^2$. The energy transferred to X-particles in the solar core per unit time is about

$$L_X^{internal} \sim \frac{4\pi\alpha^3\alpha'}{3m_e^2} n_e^2 R_c^3 E_X v_e \approx 10^{44} \alpha_{11} \,\text{erg/s}\,,$$
 (2.1)

where $n_e = 6 \cdot 10^{25}/\text{cm}^3$ is the density of electrons in the solar core, $R_c \approx 10^{10}$ cm is the core radius, $E_X \sim \text{keV}$ is the X energy, and $v_e \sim (T_c/m_e) \approx 0.05$ is the thermal velocity of electrons in the solar core. However, the mean free path of X-particles is much shorter than R_c and their emission is suppressed by the factor $(l_{free}/R_c)^2$. The mean free path due to eX-scattering can be estimated as

$$l_{free} = (\sigma_{eX} v_X n_e) , \qquad (2.2)$$

where $\sigma_{eX} = 4\pi\alpha\alpha' L/(m_X^2 v_X^4)$ is the Coulomb-like transport cross-section, and L is the Coulomb logarithm. Taking $m_X = 0.3$ keV and $v_X \sim 1$, we find $l_{free} \approx (4/L)$ cm. Correspondingly the solar luminosity due to radiation of X-particles would be below $10^{-8} L_{\odot}$, where $L_{\odot} = 4 \cdot 10^{33}$ erg/sec is the solar luminosity.

The X-luminosity of white dwarfs (WD) can be estimated similarly. The electron density inside WD is 10^4 larger than the solar one, while the radius is 10 times smaller than R_c . So $L_X^{internal}$ would be 10^5 times larger. However the mean free path of X-particles would be 10^3 times smaller. The factor 10^{-4} comes from the larger n_e and factor 10 comes from smaller eX-cross-section because of larger X energy. So finally the X-particle luminosity of white dwarfs would be about 10^{26} erg/sec, which looks safe.

There is a competing process of X-production for WD, namely decay of plasmons into the $X\bar{X}$ -pairs, because the plasma frequency in WD is about 10 keV and so it may be larger than m_X . However this process is less efficient than X-production in the above discussed reaction or at most comparable. Similar situation takes place in red giants.

Note that surprisingly strong limit $\alpha' < 10^{-30}$ for $m_X < 10$ keV was obtained from the stellar cooling in ref. [15]. However, this bound is valid if $\alpha' < 10^{-18}$ is granted. The authors of ref. [15] assumed the validity of the last bound using BBN considerations. In our approach this BBN bound is invalid since we look if it is possible to allow millicharged dark matter particles at the expense of some additional modification of BBN, e.g. by introduction of neutrino asymmetry.

2.3 Cosmological bounds

Late annihilation of X-particles, when they go out of chemical equilibrium with photons may distort the energy spectrum of CMB. The noticeable deviations from equilibrium occurred at $T \sim m_X/10$, when the bulk of X-particles was annihilating. At this temperatures the energy density of X-particles is of the order of $4\cdot 10^{-2}\,\Omega_X/m_1$ of the energy density of the CMB photons. Kinetic equilibrium of energetic photons, created in $X\bar{X}$ -annihilation, is restored by the elastic γ e-scattering very quickly, with the characteristic time of approximately $4\,(\text{keV}/T)^3$ sec. However, chemical equilibration of photons demands inelastic reaction $\gamma\,e\to 2\gamma\,e$ whose probability is approximately five orders of magnitude smaller, so the effective reaction time is about $4\cdot 10^5$ sec at $T=1\,\text{keV}$. It is quite close to the cosmological time at this temperature. As is known [16], large non-equilibrium energy influx, of the same order of magnitude as the energy density of CMB, into the cosmological plasma would be perfectly thermalized if it took place at $z>10^7$. Smaller influx could be thermalized at lower T, so the chemical potential of the CMB photons could be presumably reduced below the observational bound $\mu<10^{-4}\,T$.

The fraction of X-particles which were annihilating during recombination at $T \approx 0.2$ eV equals to 0.2 eV/ $(m_X/10) \sim 10^{-3}$ (for S-wave and even smaller for P-wave annihilation). Therefore, the energy fraction of keV photons will be 10^{-3} times the ratio of energy densities of X-particles and photons during this epoch. If Ω_X is, say, 0.1 of the baryonic contribution to Ω , then the corresponding perturbation of the chemical potential will not exceed 10^{-4} , and therefore will not exceed observational bounds. Taking into account that spectrum distortions appear only after photon degradation in energy, down from keV to the CMB energy, we see that the fraction of X-particles can be even higher.

Another very interesting and important bounds are coming from the analysis of CMBR anisotropies in the presence of millicharged particles [17]. One concludes that the fraction of such particles cannot be too large at the recombination if they are coupled to radiation.

This bound is not really restrictive in our situation since we are not assuming here that millicharged particles constitute significant fraction of matter presently.

3 BBN in the presence of milli-charged particles

3.1 Very light dark matter, $m_X < m_e$

3.1.1 Cosmological abundance

Light charged particles will be in thermal equilibrium with electromagnetic plasma in the early Universe when

$$\sigma(e^+e^- \to X\bar{X}) n_e > H, \tag{3.1}$$

where

$$H = \sqrt{\frac{8\pi^3 g_*}{90}} \frac{T^2}{m_{Pl}} \approx \frac{5T^2}{m_{Pl}}$$
 (3.2)

is the Hubble parameter at the radiation dominated cosmological stage and $n_e \sim T^3$ is the number density of electrons. Parameter $g_* = 10.75 + (7/4)(N_{eff} - 3)$ counts the number of particle species at $m_e < T < m_\mu$. The cross-section of $X\bar{X}$ production by electron-positron pairs for high electron energy, $E_e > m_e$, is

$$\sigma(e^+e^- \to X\bar{X}) \sim \alpha \alpha'/T^2,$$
 (3.3)

where $\alpha' = (e')^2/4\pi$. So the process is in equilibrium roughly at $m_e < T < \alpha \alpha' m_{Pl}$ and we expect that at $T \sim 1$ MeV X-particles have the equilibrium energy density, corresponding to one neutrino species up to the Bose-Fermi factors.

The late time (frozen) cosmological density of X-particles is determined by their annihilation into two photons and according to the standard calculations, see e.g. [8], is equal to

$$n_X^c \approx \frac{10n_\gamma \ln[\sigma(X\bar{X} \to 2\gamma)v_X m_X m_{Pl}]}{\sigma(X\bar{X} \to 2\gamma)v_X m_X m_{Pl}},$$
 (3.4)

where v_X is the center-of-mass velocity of X-particles and

$$v\sigma(X\bar{X} \to 2\gamma) = \pi(\alpha')^2/m_X^2. \tag{3.5}$$

So the mass density of X-particles at the present time, if they are stable, should be equal to

$$\rho_X^c = 10 \,\text{keV/cm}^3 \, \left(\frac{m_1}{\alpha_{11}}\right)^2 \, [1 + 0.12 \, \ln(\alpha_{11}^2/m_1)], \tag{3.6}$$

where $m_1 = m_X/\text{keV}$ and $\alpha_{11} = \alpha'/10^{-11}$. For comparison, the present day total cosmological energy density is about 5 keV/cm^3 .

Estimating ρ_X^c we have neglected the plasmon decay $\gamma_{pl} \to X\bar{X}$. This is justified because at high temperatures, $T > m_e$, when the plasma frequency, $\omega_{pl} \sim 0.1T$, exceeds m_X an account of the plasmon decay slightly shifts equilibrium condition for X-particles which are in equilibrium anyhow. At smaller temperatures, $T < m_e$, when $X\bar{X}$ -annihilation is frozen, the plasma frequency is either Bolzmann suppressed, $\sim \exp(-m_e/m_X)$, or suppressed by the smallness of α' and the plasmon decay may be neglected.

3.1.2 Qualitative discussion of BBN

Let us return now to evolution of X, e^{\pm} , and photons at BBN. We assume that X-particles do not have anomalously strong interactions with neutrinos (though this possibility may be interesting) and thus at T below 1 MeV neutrinos are decoupled from X and the electromagnetic part of the primeval plasma. Due to reaction $e^+e^- \to X\bar{X}$ and elastic scattering X-particles remain in good thermal contact with electrons and positrons. Indeed, the ratio of the reaction rate to the Hubble parameter is

$$\frac{1}{H}\frac{\dot{n}_X}{n_X} = \frac{\pi\alpha\alpha' n_e^2 \, m_{Pl}}{5m_e^2 n_X T^2} \tag{3.7}$$

and it is much larger than unity even for $T \ll m_e$, when the electron number density is exponentially suppressed. Correspondingly e^+e^- -annihilation equally well heats up photons and X-particles. So the entropy of electron-positron pairs which in the usual case was totally transferred to photons, is now distributed between γ , X, and \bar{X} . Correspondingly the entropy factor, which in the standard model was 11/4, now becomes 15/8 (assuming that X have spin zero). Hence the relative energy density of one neutrino species with respect to photons after e^+e^- -annihilation instead of $(7/8)(4/11)^{4/3}=0.227$ would become $(7/8)(8/15)^{4/3}=0.378$. However, this change takes place asymptotically at $T\ll m_e$ but at $T\sim m_e$ the effect is much smaller, which can be easily estimated analytically.

This rise of relative neutrino density has two-fold effect on BBN. First, rising density of ν_e would shift the temperature of neutron-proton freezing to smaller values and thus leads to a decrease of N_{eff} . On the other hand, the rise of the energy density of relativistic species increases N_{eff} through the corresponding increase of the Hubble parameter at the same temperature. At the moment of n/p-freezing the first effect is stronger but later on the second effect dominates. It is especially pronounced in its impact on the time of the onset of BBN. The formation of first light elements started roughly at

$$T_{BBN} \approx E_b / \ln(1/\eta) \approx 70 \,\text{keV},$$
 (3.8)

where η is the ratio of baryon to photon number densities, $\eta = n_B/n_\gamma$. The time when T_{BBN} is reached is determined by the number of relativistic species in the plasma according to $t_{BBN} \sim 1/(\sqrt{g_*}T)$. Now t_{BBN} becomes considerably shorter and less neutrons have time to decay prior to BBN. It can be described as quite large rise of N_{eff} . Below we present numerical calculations of primordial nuclei production for very light X-particles with $m_X < T_{BBN}$ which are in very good agreement with our simple analytical estimates.

The baryon-to-photon ratio at BBN in this model is different from that determined from CMBR. The latter, according to WMAP observations, is $\eta=6.19\times 10^{-10}$ [18]. We can determine η_0 at the moment of n/p-freezing, which takes place at $T\approx 0.7$ MeV using entropy conservation. Annihilation of N extra degrees of freedom into photons during the epoch between BBN and recombination dilutes η by the factor of (2+N)/2. Therefore, the baryon-to-photon ratio right after e^+e^- annihilation should be larger by this factor as compared to the standard cosmological model. Annihilation of e^+e^- pairs leads to dilution factor of (11+2N)/(4+2N). The product of these two factors determines the initial condition for the baryon-to-photon ratio:

$$\eta_0 = \frac{11 + 2N}{4} \,\eta. \tag{3.9}$$

In particular, with one charged extra scalar N=2 and $\eta_0=(15/4)\,\eta$, while in the standard model this ratio is $\eta_0^{(st)}=(11/4)\,\eta$. One should keep in mind however, that in the standard

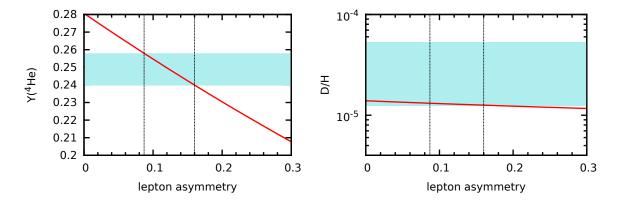


Figure 1. Left panel: Helium abundance vs lepton asymmetry in our model is shown by solid curve. Gray band indicates observationally allowed range of helium abundance. Range of χ , required to match observations, is shown by vertical dotted lines. Right panel: Deuterium abundance vs lepton asymmetry. Gray band indicates observationally allowed range of D/H. Vertical dotted lines are from the left panel.

model η changes to its asymptotic value determined by CMB in the interval from n/p-freezing down to almost complete e^+e^- -annihilation, which takes place before $T=T_{BBN}$, while in our scenario the ultimate entropy release from $X\bar{X} \to 2\gamma$ takes place at $T \sim m_X \ll T_{BBN}$.

The ratio of the neutrino temperature to the photon one at n/p-freezing in our model remains the same as in the standard case, $T_{\nu}/T_{\gamma} = (4/11)^{1/3} = 0.71$, while after e^+e^- -annihilation but prior to T_{BBN} it rises as

$$T_{\nu} = \left(\frac{4+2N}{11+2N}\right)^{1/3} T_{\gamma},\tag{3.10}$$

so for scalar X-particles it would be $T_{\nu}/T_{\gamma}=(8/15)^{1/3}=0.81$. Subsequently after $X\bar{X}$ -annihilation to photons this ratio drops down by $[2/(2+N)]^{1/3}$ and turns to $T_{\nu}/T_{\gamma}=[4/(11+2N)]^{1/3}$ which for N=2 becomes $T_{\nu}/T_{\gamma}=0.64$. In other words, the energy density of neutrinos determined by CMB would be 1.5 smaller than in the standard model.

3.1.3 Numerical results

We have calculated abundances numerically. To this end we have modified accordingly the publicly available numerical code of Kawano [19], so that all effects mentioned above are automatically taken into account.

Following Refs. [20, 21] we use the conservative constraints on light elements abundances

$$0.240 < Y_p < 0.258, (3.11)$$

$$1.2 \cdot 10^{-5} < D/H < 5.3 \cdot 10^{-5}, \tag{3.12}$$

$$0.57 < {}^{3}He/D < 1.52,$$
 (3.13)

$$^{7}Li/H > 0.85 \times 10^{-10}.$$
 (3.14)

Without lepton asymmetry the He abundance turns out to be in clear conflict with observations. In the standard model it is BBN which gives the strongest constraints on asymmetry between neutrinos and antineutrinos. Due to strong mixing between different

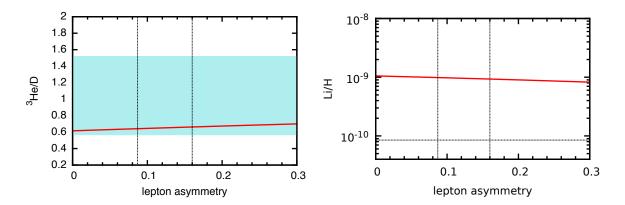


Figure 2. Left panel: ³He/D ratio vs lepton asymmetry. Gray band indicates observationally allowed range of this ratio. Vertical dotted lines are from Fig. 1. Right panel: Li/H ratio vs lepton asymmetry. Observationally allowed range is above horizontal dotted line.

neutrino species chemical potentials in all neutrino sectors are the same and in the standard model they are bounded from above as $\chi \equiv \mu/T < 0.07$ [22].

In the present case, on the contrary, we can introduce lepton asymmetry to bring Helium abundance in accord with observations.

Calculated He abundance as a function of χ is shown in Fig. 1, left panel, for the case of charged scalar, N=2. Colored band represents the range given by inequality (3.11), which in turn determines the required range of χ shown by vertical dotted lines.

Corresponding results for D/H, ³He/D and Li/H ratios are shown in Figs. 1 and 2. As we see, ther calculated ratios are marginally consistent with conservative constraints (3)-(6). We should stress that ⁷Li abundance in our model is about 50% above the standard BBN predictions. This worsens the standard model problem with ⁷Li and we need even more stellar depletion that is typically invoked.

3.2 Heavier dark matter, $m_X > m_e$

Situation becomes very much different for heavier X-particles, especially if $m_X > m_e$, and was studied in detail in Ref. [7]. In this case the cosmological number density of X-particles would be determined by their annihilation into e^+e^- . Taking for the annihilation cross-section the approximate expression

$$v\sigma(X\bar{X} \to e^+e^-) = \pi\alpha\alpha'\tau/m_X^2,$$
 (3.15)

where $\tau = \sqrt{1 - 4m_e^2/m_X^2}$ and assuming for simplicity that $m_X \gg m_e$, we find:

$$\rho_X^c \approx 2 \cdot 10^{-2} \frac{\text{keV}}{\text{cm}^3} \left(\frac{m_3^2}{\alpha_{11}} \right) [1 + 0.05 \ln(\alpha_{11}/m_3)],$$
 (3.16)

where $m_3 = m_X/\text{MeV}$.

If m_X is sufficiently small, such that the equilibrium number density of X-particles is non-negligible at n/p-freezing, then their presence would speed up the cosmological expansion and in this sense is equivalent to some dark radiation, though X-particles at this stage were non-relativistic or at most semi-relativistic. On the other hand, additional e^+e^- -pairs from $X\bar{X}$ -annihilation would diminish relative contribution of neutrinos with respect to photons and this results in a decrease of N_{eff} . For example for $m_X \simeq m_e$ the ratio of neutrino to

photon temperature would be $(T_{\nu}/T_{\gamma})^3 = 4/(11+2N)$ and if N=2 we obtain $T_{\nu}/T_{\gamma}=0.64$ already at BBN but not much later as it was in the case of light X-particles. So depending upon m_X the overall effect of X-particles on BBN may be of either sign. E.g., as it was shown in Ref. [7], the existence of millicharged particles in the mass range $m_X=4-10$ MeV can even improve the overall agreement between the predicted and observed $^2{\rm H}$ and $^4{\rm He}$ abundances.

4 Conclusion

We have found that assuming non-zero lepton asymmetry one may avoid the BBN upper bounds on the charge of possible light milli-charged particles. This in turn opens a way to modify the standard BBN predictions and to mimic possibly observed dark radiation. An interesting and testable feature of the model is that the values of the baryon and lepton asymmetries (i.e. the ratios n_B/n_γ and n_L/n_γ) are different at BBN and recombination epochs.

The model discussed here was stimulated by our work on the role which X-particles might play in the generation of large scale magnetic fields after hydrogen recombination [23].

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